

Table: Useful thermodynamic quantities in terms of the microcanonical, canonical and grand canonical partition functions [after Salvit, Frastai and Lawrie: Problems on statistical mech].

	Microcanonical	Canonical	Grand canonical
	$\Omega(E, V, N)$	$Z(T, V, N)$	$\Lambda(T, V, \mu)$
$\frac{S}{k}$	$\ln \Omega$	$\left( \frac{\partial(T \ln Z)}{\partial T} \right)_{V, N}$	$\left( \frac{\partial(T \ln \Lambda)}{\partial T} \right)_{V, \mu}$
F	$E - kT \ln \Omega$	$-kT \ln Z$	$kT \mu^2 \left( \frac{\partial(\mu^{-1} \ln \Lambda)}{\partial \mu} \right)_{T, V}$
U	Fixed (= E)	$kT^2 \left( \frac{\partial \ln Z}{\partial T} \right)_{V, N}$	$-\left( \frac{\partial \ln \Lambda}{\partial \beta} \right)_{\beta, \mu, V}$
N	Fixed	Fixed	$kT \left( \frac{\partial \ln \Lambda}{\partial \mu} \right)_{T, V}$
kT	$\left( \frac{\partial \ln \Omega}{\partial E} \right)_{V, N}^{-1}$	Fixed	Fixed
$\frac{\mu}{kT}$	$-\left( \frac{\partial \ln \Omega}{\partial N} \right)_{E, V}$	$-\left( \frac{\partial \ln Z}{\partial N} \right)_{T, V}$	Fixed
p	$kT \left( \frac{\partial \ln \Omega}{\partial V} \right)_{E, N}$	$kT \left( \frac{\partial \ln Z}{\partial V} \right)_{T, N}$	$\begin{cases} kT \frac{\partial \ln \Lambda}{\partial V} \\ kT \frac{\ln \Lambda}{V} \end{cases}$
$\frac{C_V}{k}$	$-\beta^2 \left( \frac{\partial^2 \ln \Omega}{\partial E^2} \right)_{V, N}^{-1}$	$\beta^2 \left( \frac{\partial^2 \ln Z}{\partial \beta^2} \right)_{V, N}$	$T \left( \frac{\partial^2 (T \ln \Lambda)}{\partial T^2} \right)_{V, \mu}$

$$\langle (N - \langle N \rangle)^2 \rangle$$

0

0

$$\left( \frac{\partial^2 \ln \Lambda}{\partial (\beta \mu)^2} \right)_{\beta, V}$$

$$\langle (E - \langle E \rangle)^2 \rangle$$

0

$$\left( \frac{\partial^2 \ln Z}{\partial \beta^2} \right)_{V, N}$$

$$\left( \frac{\partial^2 \ln \Lambda}{\partial \beta^2} \right)_{\beta \mu, V}$$